

**Prob.3.2.** Find five Petri nets which are LSRP, LSRP', LSR'P', LS'R'P', and L'S'R'P', respectively, if any, where for example LSR'P', stands for "live (L4-live), safe, non-reversible, and non-persistent". If it does not exist, write "none exist".

**Prob.3.3.** Find Petri nets which are:

- 1) B-fair and unconditionally-fair,
- 2) unconditionally-fair but not B-fair,
- 3) not B-fair nor unconditionally-fair, and
- 4) B-fair but not unconditionally-fair, if any. If not, write "none.exist".

**Prob.3.4.** Find the synchronic distances  $d_{12}$ ,  $d_{13}$ ,  $d_{23}$ ,  $d_{01}$ ,  $d_{02}$ , and  $d_{03}$  for the Petri net shown in Fig.3.2.

**Prob.3.5.** Find a Petri net containing transitions that are dead, strictly L1-live, strictly L2-live, strictly L3-live, and L4-live similar to the one shown in Fig.3.2 but a different one. Hint: you may use arc weights greater than one. [Wang]

**Prob.3.6.** Determine if each statement is true or false. If false, give a counter example. If true, give an example that makes you think true. [Meng]

- (a) A firing sequence  $\sigma$  is unconditionally fair if and only if any two transitions in  $\sigma$  are in a B-fair relation.
- (b) If a Petri net has one strictly L1-live transition, then the net is non-reversible.
- (c) If a Petri net is live and persistent, then the net is not B-fair.

**Prob.3.7.** Modify all the unbounded nets shown in Fig. 3.4 so as to make them bounded with minimal addition of tokens, arcs, places, and/or transitions, while keeping liveness properties same. [Yamamoto]