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Step 2.2. If M is identical to a marking on the path from the root to M, then tag M "old" and go to another new marking.

- Step 2.3. If no transitions are enabled at M, tag M "dead-end".
- Step 2.4. While there exist enabled transitions at M, do the following for each enabled transition t at M:
  - Step 2.4.1. Obtain the marking M' that results from firing t at M.
  - Step 2.4.2. On the path from the root to M' if there exists a marking M" such that  $M'(p) \ge M''(p)$  for each place p and  $M' \ne M''$ , i.e. M" is coverable, then replace M'(p) by  $\omega$  for each p such that M'(p) > M''(p).
  - Step 2.4.3. Introduce M' as a node, draw an arc with label t from M to M', and tag M' "new".

**Example 4.1** Consider the net shown in Fig. 3.2. For the initial marking  $M_0 = (1\ 0\ 0)$ , the two transitions  $t_1$  and  $t_3$  are enabled. Firing  $t_1$  transforms  $M_0$  to  $M_1 = (0\ 0\ 1)$ , which is a "dead-end" node, since no transitions are enabled at  $M_1$ . Now, firing  $t_3$  at  $M_0$  results in  $M_3' = (1\ 1\ 0)$ , which covers  $M_0 = (1\ 0\ 0)$ . Therefore, the new marking is  $M_3 = (1\ \omega\ 0)$ , where two transitions  $t_1$  and  $t_3$  are again enabled. Firing  $t_1$  transforms  $M_3$  to  $M_4 = (0\ \omega\ 1)$ , from which  $t_2$  can be fired, resulting in an "old" node  $M_5 = M_4$ . Firing  $t_3$  at  $M_3$  results in an "old" node  $M_6 = M_3$ . Thus, we have the coverability tree shown in Fig. 4.1(a).